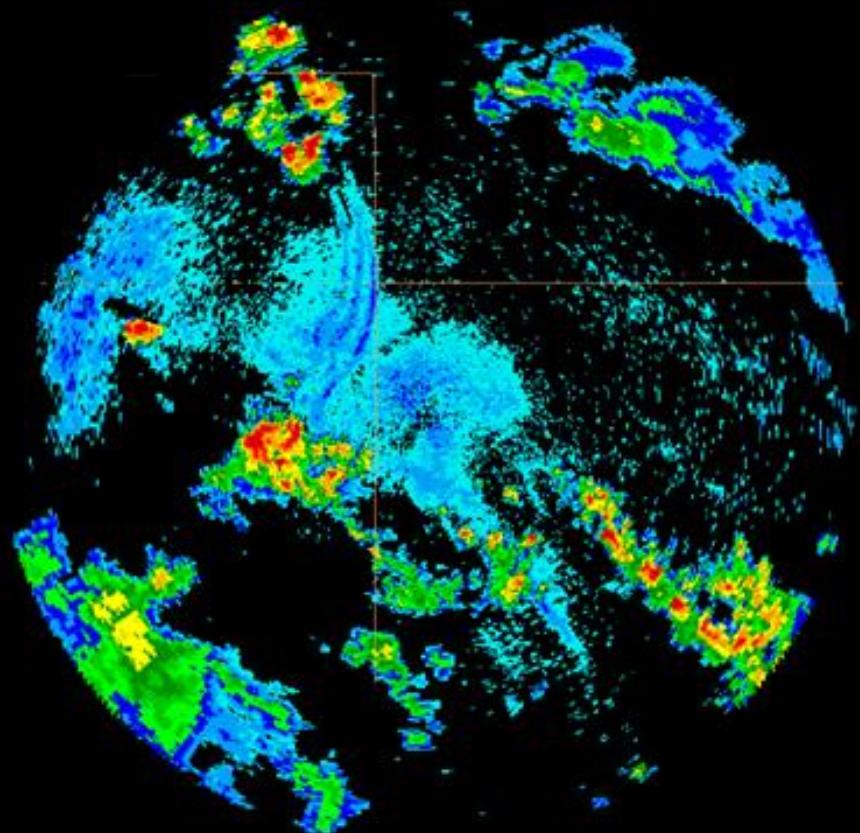


# Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

Antonio Manuel Moreno Ródenas



# 0- Index

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

1. Introduction
2. Methods
3. Case study application
4. Results and discussion
5. Conclusions.

1.-  Introduction

2.-  Methods

3.-  Case study and application

4.-  Results and Discussion

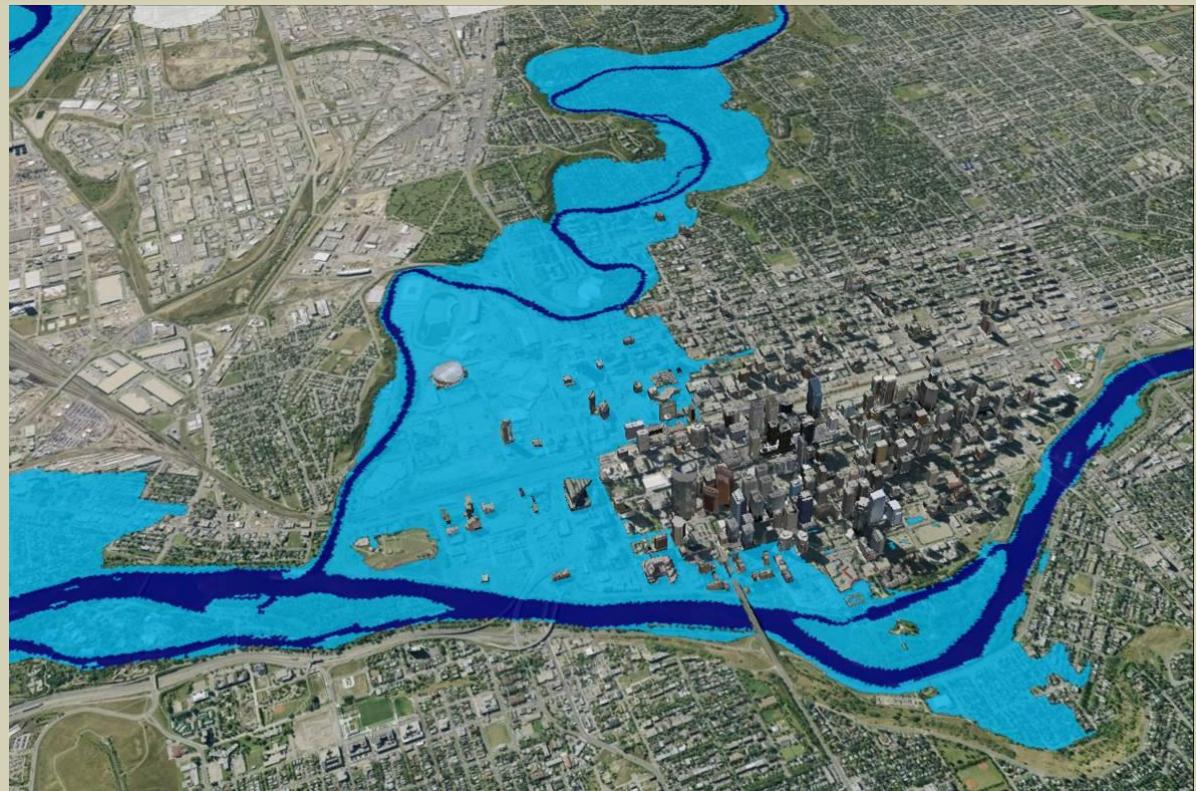
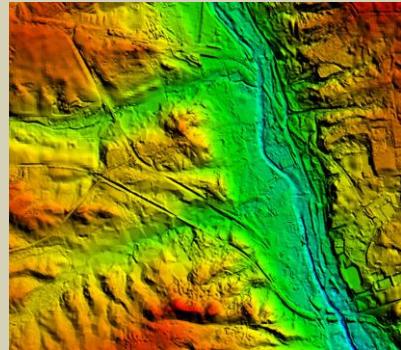
5.-  Conclusion

# 1- Introduction

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

Distributed rainfall-runoff modelling.

Demand of a high quality and resolution precipitation fields



1.-  Introduction

2.-  Methods

3.-  Case study and application

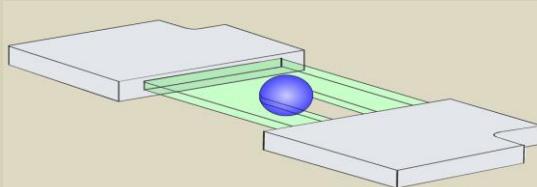
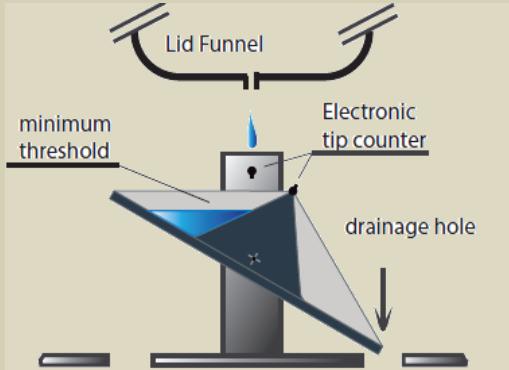
4.-  Results and Discussion

5.-  Conclusion

# 1- Introduction

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

Rain gauge / Disdrometer



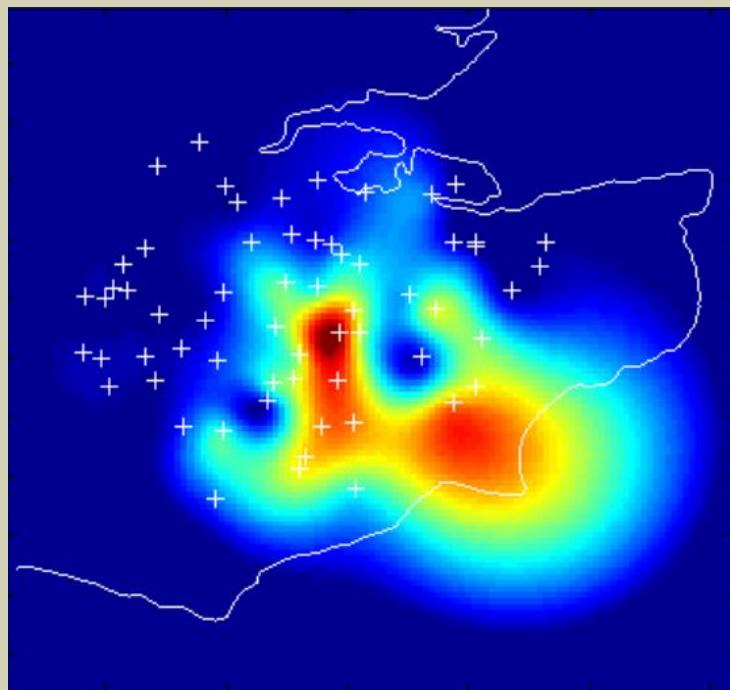
Ground based weather Radar



# 1- Introduction

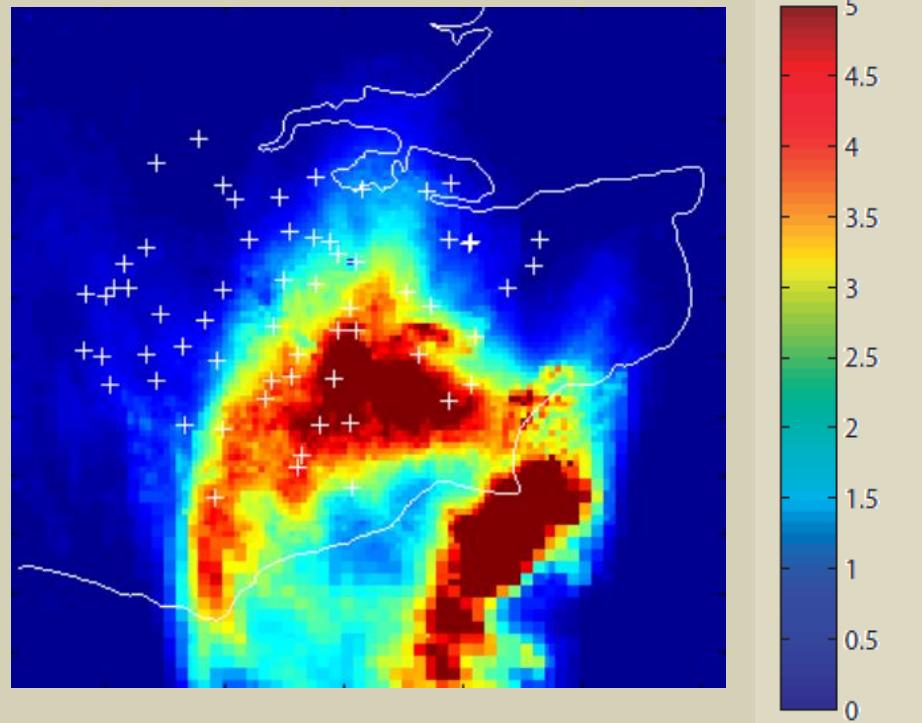
Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

Rain gauge biharmonic spline interpolation



Precipitation fields for Kent area in 20<sup>th</sup> of July, 2007 (mm/h)

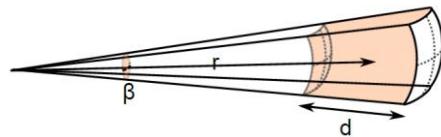
Quantitative radar estimation



# 1- Introduction

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

Radar equation :  $P_r = \frac{P_e G^2 \lambda^2 \sigma_T}{(4\pi)^3 R^4}$



Rayleigh backscattering

$$P_r = \frac{P_e G^2 \lambda^2}{(4\pi)^3 R^4} \cdot \frac{\pi \beta R^2}{4} \frac{c_o \tau}{2} \cdot \frac{\pi^5}{\lambda^4} |K|^2 \sum_V D_i^6$$

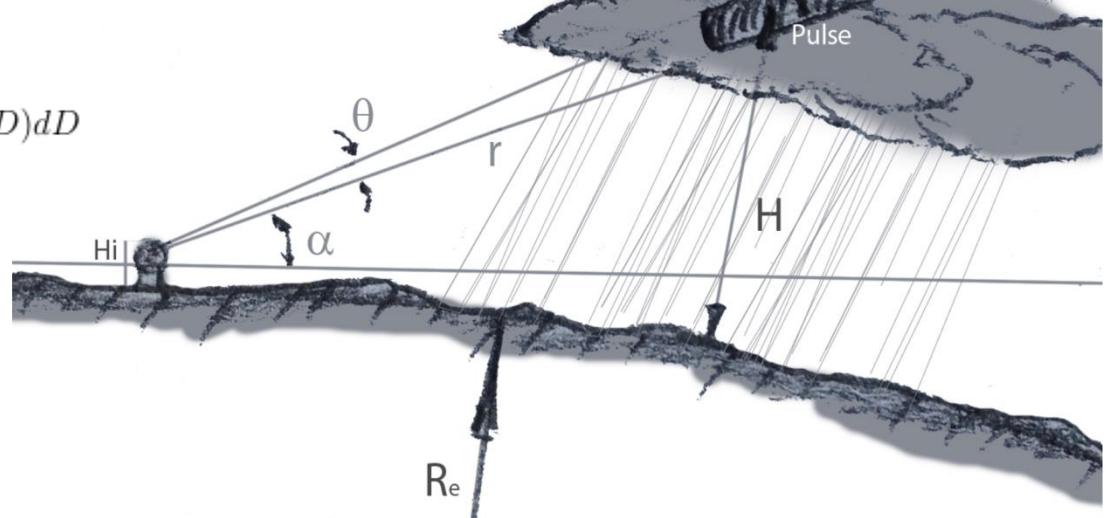
$$Z = \frac{\lambda^4}{\pi^5 |K|^2} \int_{D_{inf}}^{D_{max}} \sigma(D) N(D) dD \approx \int D^6 N(D) dD$$

$$R \approx \int D^{3.67} N(D) dD$$

$$Z = a R^b$$

$$Z = 200 R^{1.6}$$

$$\sigma_i = \frac{\pi^5}{\lambda^4} |K|^2 D_i^6 \quad |K| = \left| \frac{\epsilon - 1}{\epsilon + 2} \right|$$



1.- Introduction

2.- Methods

3.- Case study and application

4.- Results and Discussion

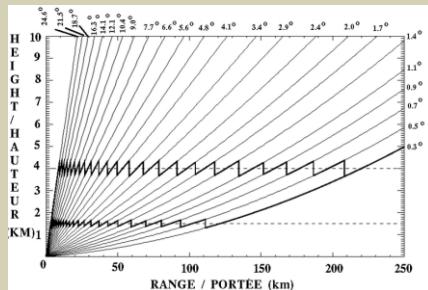
5.- Conclusion

# 1- Introduction

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

## Radar Error sources

Scanning altitude



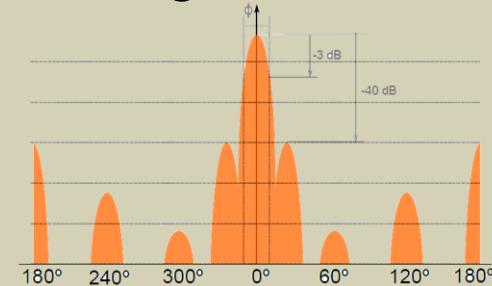
Ground clutter & Blockages

Jamming, active interference

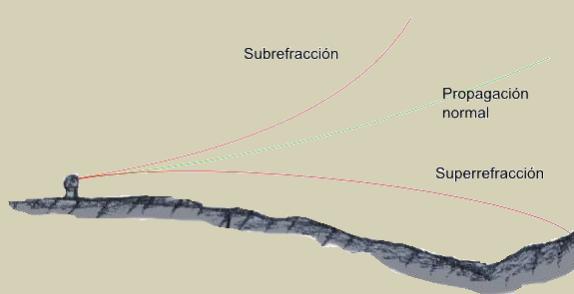
Raindrop size distribution

Attenuation

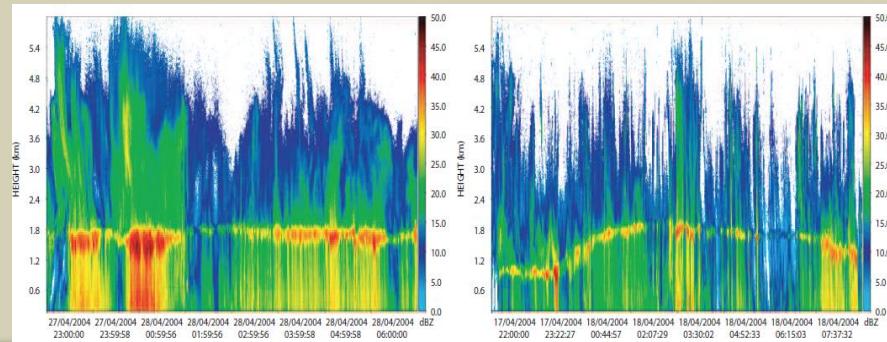
Echo origin, directionality



Anomalous propagation



Bright Band phenomena



1.- Introduction

2.- Methods

3.- Case study and application

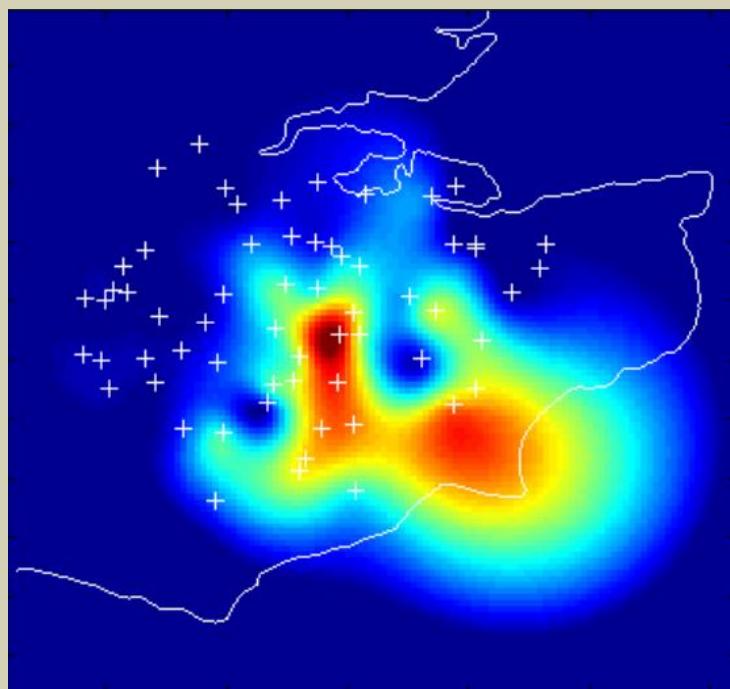
4.- Results and Discussion

5.- Conclusion

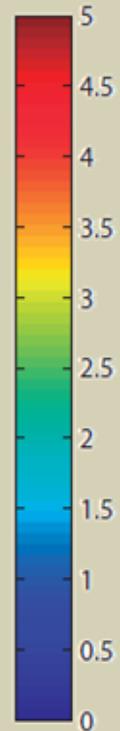
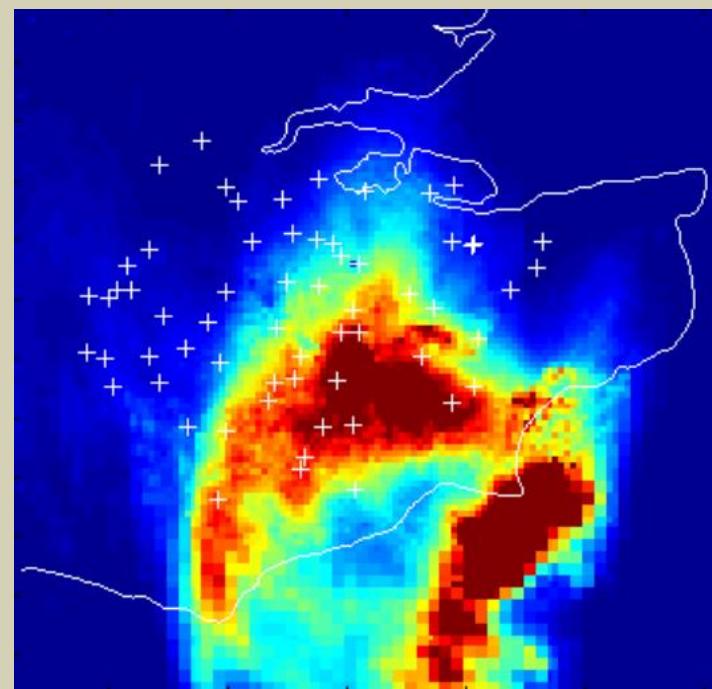
# 1- Introduction

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

Rain gauge biharmonic spline interpolation



Quantitative radar estimation



Precipitation fields for Kent area in 20<sup>th</sup> of July, 2007 (mm/h)

## 2- Methods

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

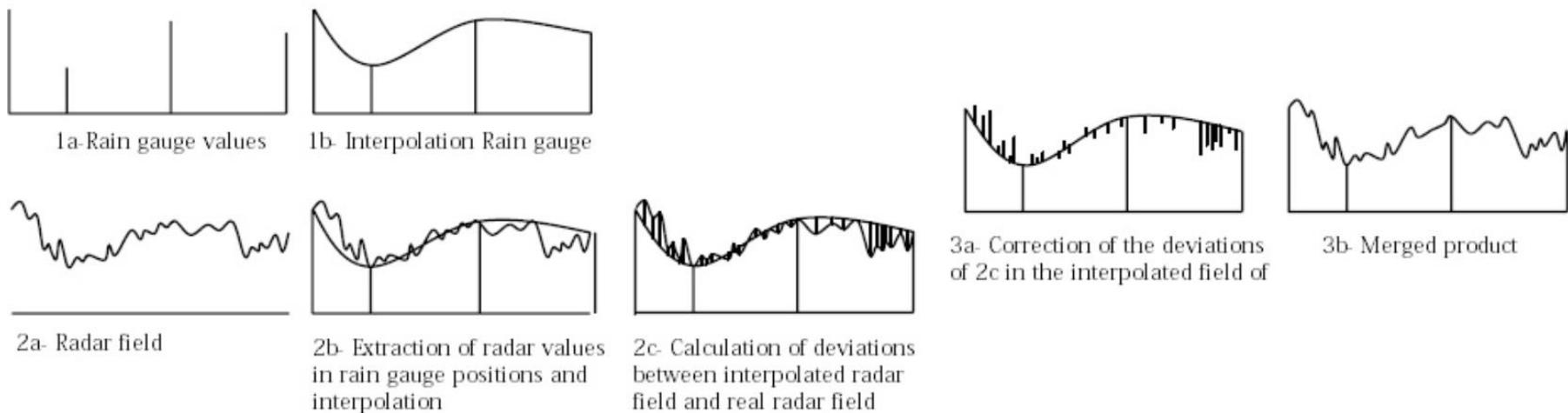
Evaluation of:

- Conditional merging (Ehret y Pegram 2002). With 3 interpolation strategies:
  - 1.-CM LI, Elastic frame fitting with linear triangulation.
  - 2.-CM V4, Biharmonic Spline interpolation.
  - 3.-KRE, Kriging with radar error, Ordinary kriging method.
- 4.- KED, multivariate Geostatistic method, Kriging with external drift

## 2- Methods

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

Conditional merging workflow (Ehret and Pegram 2002).



# 2- Methods

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

3 interpolation strategies:

1.-CMLI, Linear triangulation and elastic surface fitting.

2.-CMV4, Biarmonic spline interpolation.

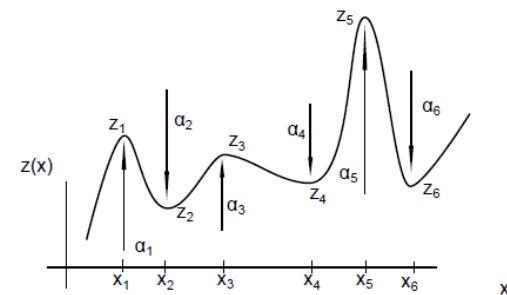
$$\nabla^4 z(x) = \sum_{j=1}^N \alpha_j \delta(x - x_j)$$

$$z(x_i) = z_i$$

$$\phi(x) = |x| 2(\ln|x| - 1)$$

$$z(x) = \sum_{j=1}^N \alpha_j |x - x_j| 2(\ln|x - x_j| - 1)$$

$$z_i = \sum_{j=1}^N \alpha_j \phi(x_i - x_j)$$



1.-  
Introduction

2.-  
Methods

3.-  
Case study and application

4.-  
Results and Discussion

5.-  
Conclusion

# 2- Methods

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

## 3.-KRE, Kriging with radar error

Kriging problem: Best linear unbiased estimator

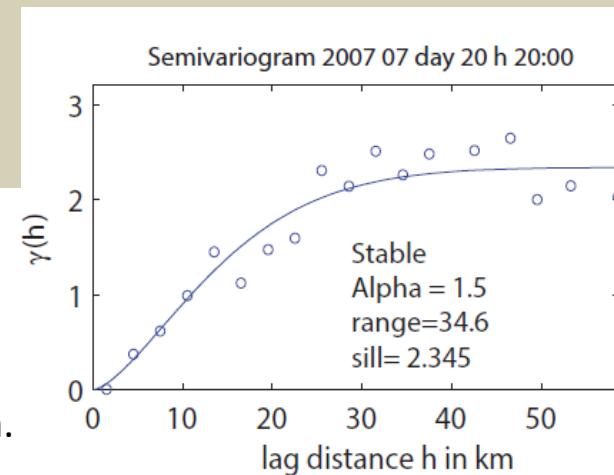
Rainfall is considered an stochastic variable.

Spatial characterization of rainfall measurements (rain gauges) R(xi)  
Semivariogram representation, “stable” structure.

$$\gamma(h) = \frac{1}{2 \cdot N(h)} \cdot \sum_{i=1}^{N(h)} (R(x_i) - R(x_i + h))^2$$

$$\gamma_\alpha(h) = b \cdot (1 - e^{-\frac{|h|^\alpha}{a}})$$

$\alpha = 1.5$   
a and b parameters to estimate, reflecting sill and range of the semivariogram.



1.- Introduction

2.- Methods

3.- Case study and application

4.- Results and Discussion

5.- Conclusion

## 2- Methods

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

### 3.-KRE, Kriging with radar error

$$\hat{R}(x_0) = \sum_{i=1}^n (\omega_i(x_0) \cdot R(x_i))$$

$$\begin{aligned} \sum_{j=1}^n \omega_j \gamma_{ij} + \mu &= \gamma_{i0}, \quad \forall i = 1, \dots, n \\ \sum_{i=1}^n \omega_i &= 1 \end{aligned}$$

$$\begin{bmatrix} \gamma_{1,1} & \gamma_{1,2} & \cdots & \gamma_{1,n} & 1 \\ \gamma_{2,1} & \gamma_{2,2} & \cdots & \gamma_{2,n} & 1 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ \gamma_{n,1} & \gamma_{n,2} & \cdots & \gamma_{n,n} & 1 \\ 1 & 1 & \cdot & 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} \omega_1 \\ \omega_2 \\ \vdots \\ \omega_n \\ \mu \end{bmatrix} = \begin{bmatrix} \gamma_{1,0} \\ \gamma_{2,0} \\ \vdots \\ \gamma_{n,0} \\ 1 \end{bmatrix}$$

## 2- Methods

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

KED, Kriging with external drift. (kriging multivariate)

Direct mix between distributed radar data and punctual rain gauge measurements.

$$E[R(x)] = \sum_{k=0}^p \beta_k f_k(x) \quad E[R(x)] = \beta_0 + \beta_r f_{rad}(x)$$

$$\sum_{j=1}^n \omega_j \gamma_{ij} + \mu_0 + \mu_r \cdot Z_i = \gamma_{i0}$$

$$\sum_{i=1}^n \omega_i = 1$$

$$\sum_{j=1}^n \omega_j Z_j = Z_0$$

$$\begin{bmatrix} \gamma_{1,1} & \gamma_{1,2} & \cdots & \gamma_{1,n} & Z_1 & 1 \\ \gamma_{2,1} & \gamma_{2,2} & \cdots & \gamma_{2,n} & Z_2 & 1 \\ \vdots & \vdots & \ddots & \vdots & \vdots & \vdots \\ \gamma_{n,1} & \gamma_{n,2} & \cdots & \gamma_{n,n} & Z_n & 1 \\ Z_1 & Z_2 & \cdot & Z_n & 0 & 0 \\ 1 & 1 & \cdot & 1 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} \omega_1 \\ \omega_2 \\ \vdots \\ \omega_n \\ \mu_r \\ \mu_0 \end{bmatrix} = \begin{bmatrix} \gamma_{1,0} \\ \gamma_{2,0} \\ \vdots \\ \gamma_{n,0} \\ Z_0 \\ 1 \end{bmatrix}$$



### 3- Case study

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

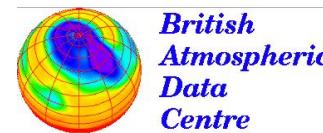
-Application of the 4 algorithms to 6 storm data sets from July 2007 in Kent, England

- 1 - Data quality processing
- 2- Selection and storm classification (convective/stratiform)
- 4- Merging for hourly accumulation
- 3- Cross comparison of the data using RG as reference values  
Bias, RMSE, Correlation coeff, Ratio of variances

Data:

73 Tipping bucket rain gauge  
0.2 mm Volume threshold

Radar C-Band composite (NIMROD PROJECT)  
1 km<sup>2</sup>, 5min



1.- Introduction

2.- Methods

3.- Case study and application

4.- Results and Discussion

5.- Conclusion

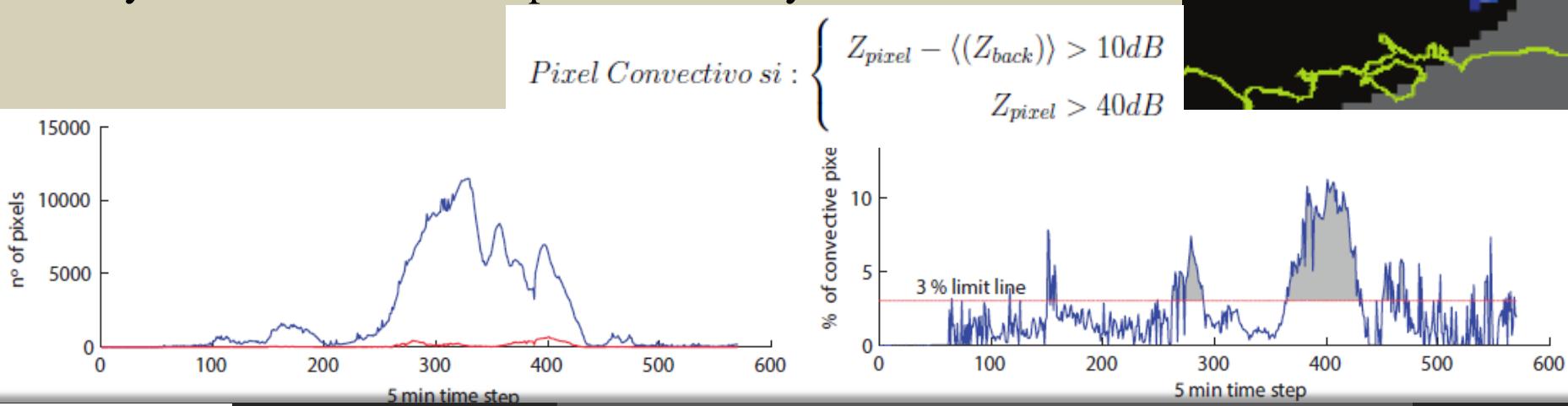
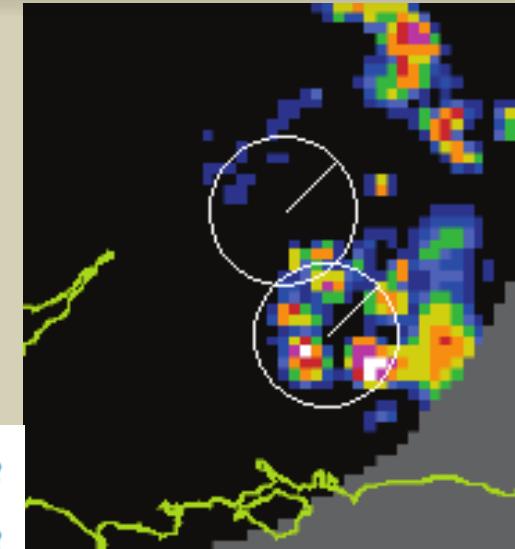
# 3- Case study

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

## Storm classification

Importance of Convective-stratiform convective, DSD.  
Possible interaction with the algorithms.

Development of the 2D classifier algorithm.  
Study of the backscattered power intensity.



- 1.- Introduction
- 2.- Methods
- 3.- Case study and application
- 4.- Results and Discussion
- 5.- Conclusion

### 3- Case study

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

#### Storm Classification.

Storm nº	Date (2007 07)	Time frames	nº RG	Maximum accumulated rainfall (mm)			Type
				RG	Radar at RG	Radar field	
1	04 09:00 - 05 00:00	16 h	62	7.6	14.1	21.2	C
2	05 12:00 - 06 01:00	14 h	62	4.6	2.9	4.57	S
3	19 21:00 - 20 14:00	18 h	62	54.8	39.8	83.3	C
4	23 10:00 - 24 01:00	16 h	62	29.6	20.9	29.4	S
5	27 16:00 - 28 04:00	13 h	62	6.8	4.1	9.7	S
6	28 18:00 - 29 09:00	16 h	62	20	8.2	23.5	S

# 4- Results and discussion

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

Storm 1	Bias	RSME	Corr	RVar
Method	(mm/h)	(mm/h)	(-)	(-)
Radar	0.05	0.88	0.48	0.53
KRE	-0.17	1.11	0.289	1.32
CMV4	-0.244	1.43	0.17	2.26
CMLI	-0.259	1.45	0.169	2.31
KED	-0.1739	0.828	0.426	0.507

Storm 3	Bias	RSME	Corr	RVar
Method	(mm/h)	(mm/h)	(-)	(-)
Radar	-0.41	2.71	0.84	0.33
KRE	-0.054	1.62	0.938	1.09
CMV4	-0.039	1.62	0.937	1.07
CMLI	-0.05	1.62	0.938	1.07
KED	-0.028	1.477	0.947	1.05

Storm 5	Bias	RSME	Corr	RVar
Method	(mm/h)	(mm/h)	(-)	(-)
Radar	-0.43	0.63	0.56	0.26
KRE	-0.076	0.404	0.734	0.82
CMV4	-0.067	0.44	0.71	1.04
CMLI	-0.06	0.449	0.701	1.05
KED	-0.0785	0.383	0.758	0.755

Storm 2	Bias	RSME	Corr	RVar
Method	(mm/h)	(mm/h)	(-)	(-)
Radar	-0.11	0.37	0.02	1.13
KRE	-0.06	0.179	0.76	1
CMV4	-0.05	0.18	0.766	1.2
CMLI	-0.052	0.1878	0.762	1.23
KED	-0.0655	0.16	0.79	0.866

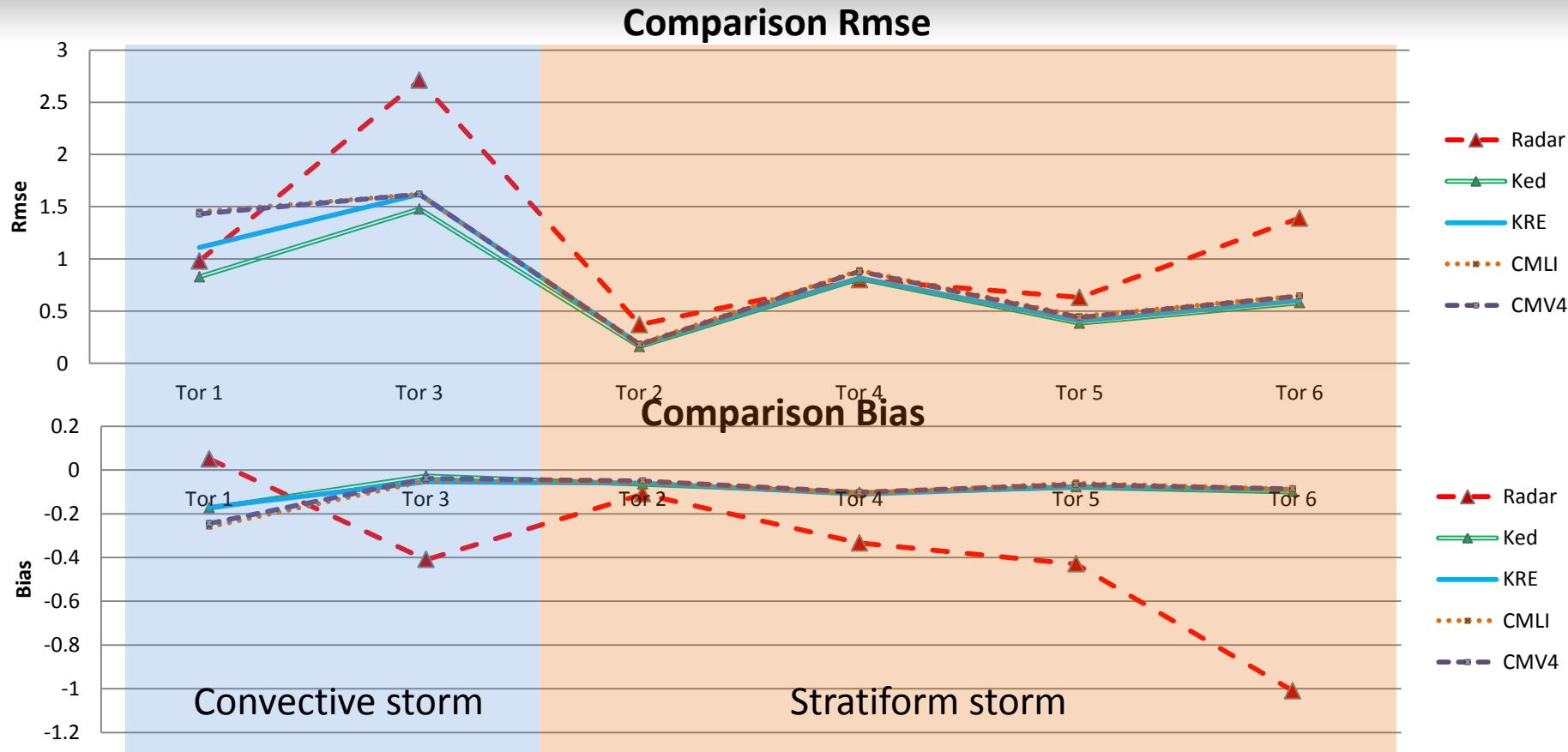
Storm 4	Bias	RSME	Corr	RVar
Method	(mm/h)	(mm/h)	(-)	(-)
Radar	-0.334	0.8	0.86	0.48
KRE	-0.11	0.819	0.82	0.96
CMV4	-0.102	0.88	0.8	1.05
CMLI	-0.106	0.89	0.79	1.05
KED	-0.1037	0.81	0.82	0.99

Storm 6	Bias	RSME	Corr	RVar
Method	(mm/h)	(mm/h)	(-)	(-)
Radar	-1.01	1.39	0.27	0.117
KRE	-0.09	0.6	0.8	0.89
CMV4	-0.086	0.645	0.79	1.03
CMLI	-0.088	0.647	0.79	1.04
KED	-0.1	0.58	0.81	0.87

# 4- Results and discussion

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

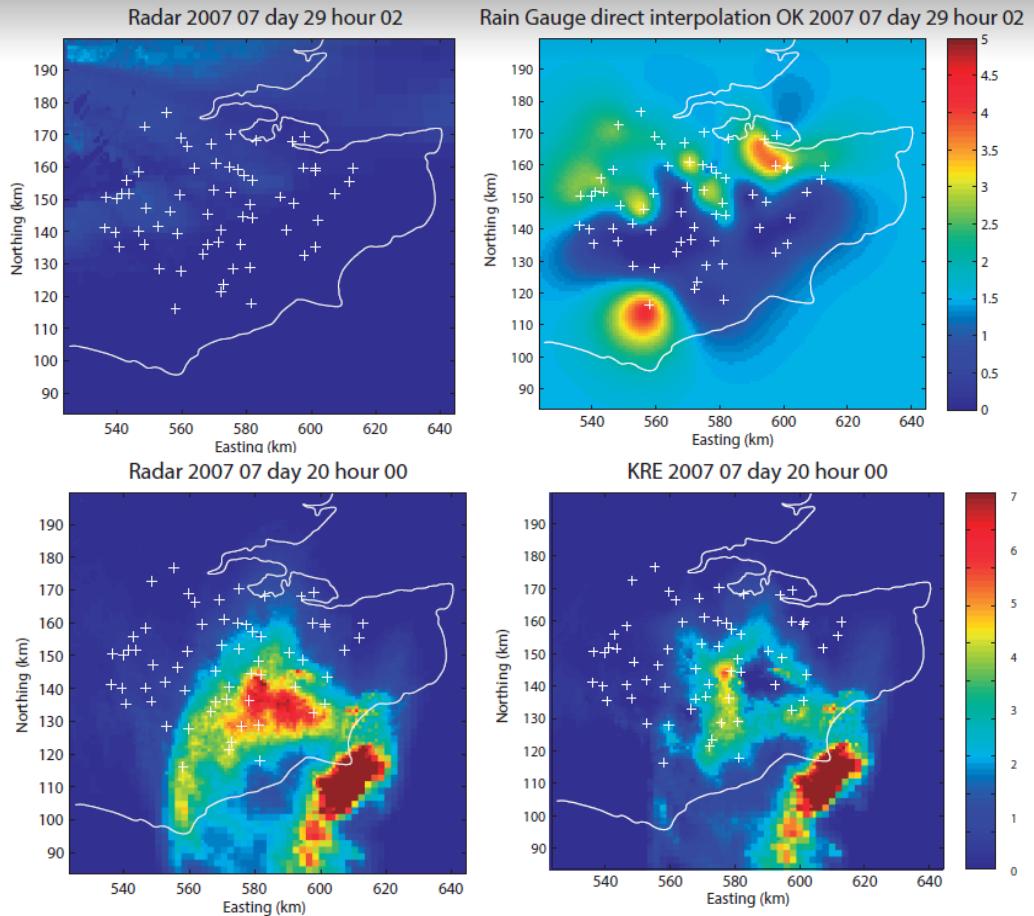


# 4- Results and discussion

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

## Instabilities in the method:

- Bad initial conditioning.
- High influence of the rain gauges errors.



## Developments proposed:

- Radar feeded filters for rain gauge errors.
- Non-parametric semivariograms.

1.- Introduction

2.- Methods

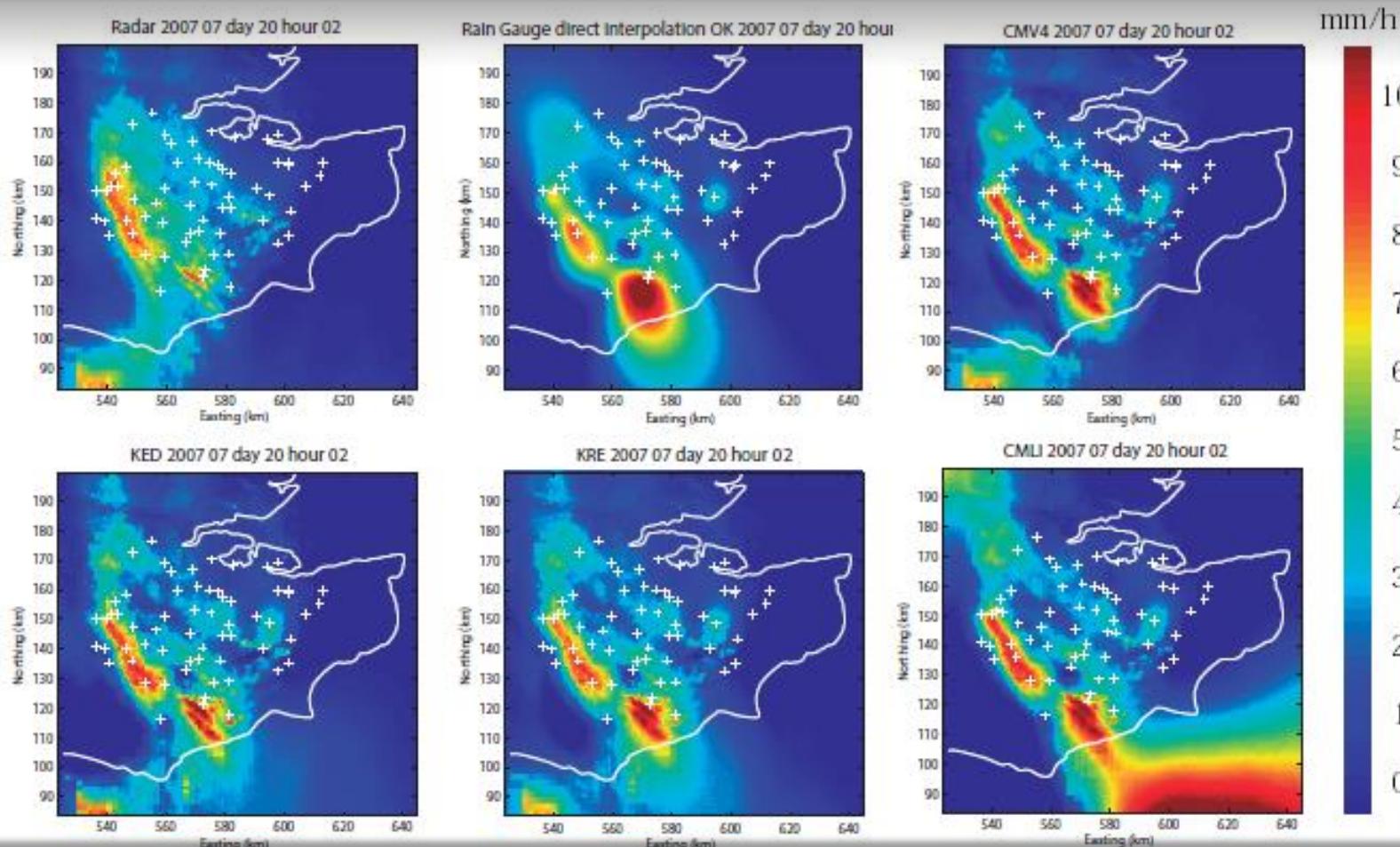
3.- Case study and application

4.- Results and Discussion

5.- Conclusion

# 4- Results and discussion

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.



1.-  
Introduction

2.-  
Methods

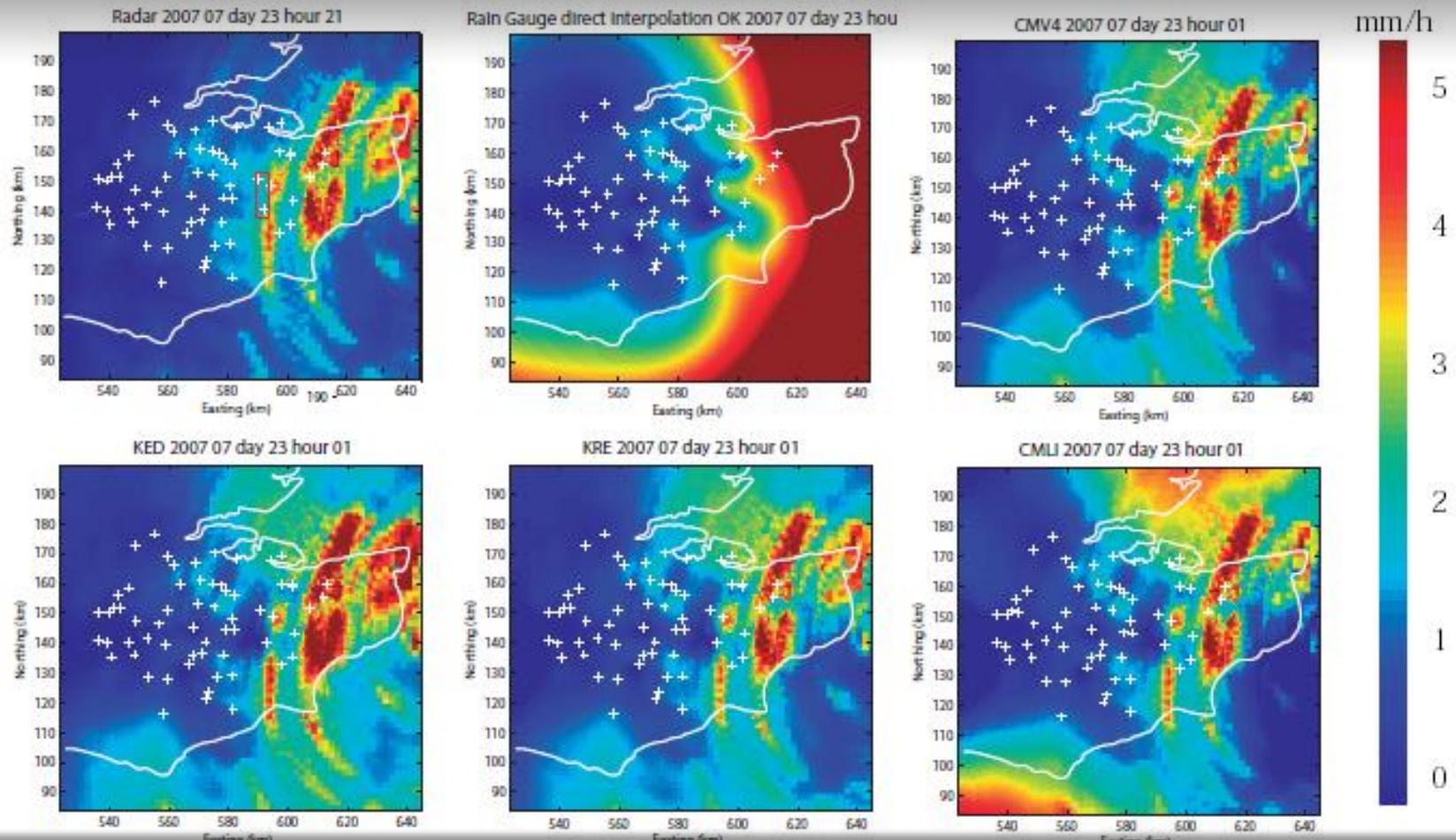
3.-  
Case study and  
application

4.-  
Results and  
Discussion

5.-  
Conclusion

# 4- Results and discussion

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.



- 1.- □ Introduction
- 2.- □ Methods
- 3.- □ Case study and application
- 4.- ■ Results and Discussion
- 5.- □ Conclusion

# 5- Conclusions

Estimation of high spatial resolution precipitation fields using merged rain gauge - radar data.

- 1- The use of quality radar estimations is essential if the target is to reproduce the spatial variability of rainfall with detail ( $1\text{km}^2$ ). Application of merging techniques is still necessary since radar can present important errors.
- 2- It is necessary the use of high quality pluviometric information, since they are considered as true ground in this applications (nevertheless they are not error exempt).
- 3- CMLI and CMV4 are too often affected by merging instabilities.  
They are outperformed by KRE and KED. Both present a good representation of most rainfall structures. Still KED behave better under convective cases. This is possibly due

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THANKS FOR YOUR  
ATTENTION

